

Slope of a Polar Curve

Find the slope of the cardioid $r = 2(1 + \cos\theta) = f(\theta)$
@ $r = \theta/6$

$$x = r \cos\theta$$

$$y = r \sin\theta$$

$$r = -2 \sin\theta$$

$$\frac{dy}{dx} = \frac{dy/d\theta}{dx/d\theta} = \frac{f'(\theta)\sin\theta + f(\theta)\cos\theta}{f'(\theta)\cos\theta - f(\theta)\sin\theta}$$

$$= \frac{(-2\sin\theta)\sin\theta + 2(1+\cos\theta)\cos\theta}{(-2\sin\theta)\cos\theta - 2(1+\cos\theta)\sin\theta}$$

$$\theta = \pi/6 \quad \frac{dy}{dx} = -1$$